INTRODUCTION

One of the most widely used block cipher algorithms is the Data Encryption Standard (DES), adopted in 1977 by the American National Standards Institute (ANSI).

After more than twenty years of use with continuous aging due to advances in cryptography, the National Institute of Standards and Technology (NIST) on September 12, 1997, started a process to stimulate the development and submission of alternatives to the DES. Twenty-one algorithms were analyzed in the first round and five algorithms were analyzed in the second round. On October 2, 2000 the NIST announced that the new encryption technique, named Advanced Encryption Standard (AES), would use the Rijndael algorithm, designed by two well-known specialists, Joan Daemen and Vincent Rijmen from Belgium. The new AES will be used to protect sensitive information of federal computer systems, as well as many private businesses.

FUNDAMENTAL ENCRYPTION OVERVIEW

Throughout history, mankind has faced the problem of storing and transmitting sensitive information in a way that could guarantee both reliable and easy access to authorized persons and prevent undue and illegal access. This has led to the development of many ingenious methods to cipher and decipher data.

The phenomenal development of computers and expansion of digital information exchange has led to a fundamental problem related to the availability, control, and security of data. To deal with this problem, several computer based encryption technologies and standards were developed. One of the most popular methods developed is the Block Cipher.

An algorithm that uses a key is, in general, much more secure. If the algorithm itself is secure in its design, then the data is secure (as long as the key is secure) even if the encryption algorithm is known. The only way to decipher the message is through the use of the correct key.

There are two basic types of keys:
1. Symmetric
2. Public

In a symmetric key algorithm, both encryption and decryption processes use the same key, which must be kept secret. In a public key system, two keys are used: one public (used to cipher messages) and another, private and secret (used to decipher the message).
In the AES (Symmetric Key) method, the plain text is broken in several blocks of the same size. For example, the following plain text:

"I pass death with the dying and birth with new washed baby, and am not contained between my hat and boots." (Walt Whitman)

This text is broken into 16-byte (arbitrary size) chunks as shown in Example 1:

**EXAMPLE 1: PLAIN TEXT DIVIDED INTO 16-BYTE BLOCKS**

| I pass death with the dying and birth with new washed baby, and am not contained between my hat and boots | tuvwxyz |

**Note 1:** \(\backslash\) is a single character and represents End of String.

**Note 2:** Through a process called ‘padding’, an incomplete 16-byte text block may be completed using random characters like “tuvwxyz.”

Next, each block (plus an encryption key) is combined together using an algorithm that executes a complex function resulting in the production of a ciphered block. See Example 2.

**EXAMPLE 2: PLAIN TEXT BLOCK TO CIPHERED BLOCK PROCESS**

<table>
<thead>
<tr>
<th>Plain Text Block</th>
<th>+</th>
<th>Key</th>
<th>Encryption Algorithm</th>
<th>Ciphered Block</th>
</tr>
</thead>
<tbody>
<tr>
<td>I pass death with the dying and birth with new washed baby, and am not contained between my hat and boots</td>
<td></td>
<td>waltwhitman,poet</td>
<td>→</td>
<td>dfkei5k7kkko23aq</td>
</tr>
</tbody>
</table>

The deciphering process takes the encrypted block plus the encryption key and passes them through an algorithm that executes the reverse process, resulting in a plain text block. See Example 3.

**EXAMPLE 3: CIPHERED BLOCK TO PLAIN TEXT BLOCK PROCESS**

<table>
<thead>
<tr>
<th>Ciphered Block</th>
<th>+</th>
<th>Key</th>
<th>Decryption Algorithm</th>
<th>Plain Text Block</th>
</tr>
</thead>
<tbody>
<tr>
<td>dfkei5k7kkko23aq</td>
<td></td>
<td>waltwhitman,poet</td>
<td>→</td>
<td>I pass death wit</td>
</tr>
</tbody>
</table>
HOW THE AES ALGORITHM IS IMPLEMENTED IN A PIC16XXX MICROCONTROLLER

The AES Algorithm - An Overview

AES is a symmetric key block cipher algorithm that may use three different block and key sizes:

- 16-byte - 128 bits
- 24-byte - 192 bits
- 32-byte - 256 bits

The algorithm executes a series of rounds. The intermediate results of the rounds over the block are called states.

The number of round transformations is variable and a function of the sizes of the key and the text, shown as follows:

**TABLE 1: ROUND TRANSFORMATIONS REQUIRED**

<table>
<thead>
<tr>
<th>Key Size</th>
<th>16-byte block</th>
<th>24-byte block</th>
<th>32-byte block</th>
</tr>
</thead>
<tbody>
<tr>
<td>16-byte key</td>
<td>10*</td>
<td>12</td>
<td>14</td>
</tr>
<tr>
<td>24-byte key</td>
<td>12</td>
<td>12</td>
<td>14</td>
</tr>
<tr>
<td>32-byte key</td>
<td>14</td>
<td>14</td>
<td>14</td>
</tr>
</tbody>
</table>

* Chosen for implementation in this Application Note.

For these transformations, the state (block) and the key are both taken as matrixes, as shown in Table 2 and Table 3.

**TABLE 2: BLOCK MATRIX**

|----------|----------|----------|-----------|-----------|-----------|-----------|-----------|

**TABLE 3: KEY MATRIX**

|---------|---------|---------|---------|---------|---------|---------|---------|

**Note:** In the 16-byte (128-bit) implementation, both matrixes are 4x4.
Key Schedule - Expansion and Selection:
Encryption

In order to prepare for the round transformations, a "key schedule" operation must be executed. This operation uses the original key to create several round keys. Each round key, including the original one, will be used in one of the rounds.

This operation is performed in two steps:

1. Key Expansion -> takes the key from the previous round and expands it to create the key for the next round, according to the C code for 16-byte (128-bit key) shown below:

2. Round Key Selection -> takes the round buffer in blocks of 16 bytes (for 128-bit keys), so that the keys (taken in bytes) for a given round "i" are:

After the enc_key_schedule, an initial key addition must be executed:

Initial key_addition:

Before the first round of encryption, an initial key_addition is performed. This operation executes a simple XOR of the state with the initial round key. In C for 16-byte (128-bit) key and block:

C Code for 16-Byte Key Expansion

```c
KeyExpansion(byte Key[], byte W[][])
{
    byte rcon=1; // initial value of round constant
    for (j=0; j<16; j++) // first key expansion no changed
        w[0][j] = key[j];
    for(i = 1; i<11; i++)
    {
        for(j = 0; j<16; j++)
        {
            if(j<4) // calculate S_Box based values
                W[i][j] = W[i-1][j] ^ S_box(W[i-1][12+((j+1)%4)]);
            else
                W[i][j] = W[i-1][j] ^ w[i][j-4]; //
            if((j%4) == 0)
                W[i][j] ^= rcon;
        }
        rcon = xtime(rcon); // calculate rcon for next round
    }
}
```

with: `Rcon = {0x36, 0x1B, 0x80, 0x40, 0x20, 0x10, 0x08, 0x04, 0x02, 0x01};` where `Rcon` represents a vector of round constants.

The Structure of the Round Transformations: Encryption

In the encryption process, each of the ten rounds (with the exception of the last one) is composed of four stages:

- byte_sub
- shift_row
- mix_column
- key_addition

The last round doesn't execute the mix_column stage, thus the sequence is:

- byte_sub
- shift_row
- key_addition
### TABLE 4: S-BOX OR ENCRYPTION SUBSTITUTION TABLE (VALUES IN HEXADECIMAL)

<table>
<thead>
<tr>
<th>x</th>
<th>y</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>01</td>
</tr>
<tr>
<td>1</td>
<td>2B</td>
</tr>
<tr>
<td>2</td>
<td>3C</td>
</tr>
<tr>
<td>3</td>
<td>4D</td>
</tr>
<tr>
<td>4</td>
<td>5E</td>
</tr>
<tr>
<td>5</td>
<td>6F</td>
</tr>
<tr>
<td>6</td>
<td>7G</td>
</tr>
<tr>
<td>7</td>
<td>8H</td>
</tr>
<tr>
<td>8</td>
<td>9I</td>
</tr>
<tr>
<td>9</td>
<td>A0</td>
</tr>
<tr>
<td>A</td>
<td>B1</td>
</tr>
<tr>
<td>B</td>
<td>C2</td>
</tr>
<tr>
<td>C</td>
<td>D3</td>
</tr>
<tr>
<td>D</td>
<td>E4</td>
</tr>
<tr>
<td>E</td>
<td>F5</td>
</tr>
<tr>
<td>F</td>
<td>G6</td>
</tr>
<tr>
<td>G</td>
<td>H7</td>
</tr>
<tr>
<td>H</td>
<td>I8</td>
</tr>
<tr>
<td>I</td>
<td>J9</td>
</tr>
<tr>
<td>J</td>
<td>KA</td>
</tr>
<tr>
<td>K</td>
<td>LB</td>
</tr>
<tr>
<td>L</td>
<td>MB</td>
</tr>
<tr>
<td>M</td>
<td>NB</td>
</tr>
<tr>
<td>N</td>
<td>OB</td>
</tr>
<tr>
<td>O</td>
<td>PB</td>
</tr>
<tr>
<td>P</td>
<td>QA</td>
</tr>
</tbody>
</table>

### DESCRIPTION OF ENCRYPTION STAGES:

**byte_sub:**

In this stage, each byte of the block matrix is replaced by the content of the S-box at the position defined by the byte that is going to be substituted. In this case, the S-box or substitution table may be seen as a 256 byte invertible vector/matrix used to map the substitution process.

This is equivalent to the following C language fragment:

```c
for(i=0;i<BLOCKSIZE;i++)
    block[i]=S_box[block[i]];
```

### EXAMPLE 4: S-BOX SUBSTITUTION

If block[0] = 0x41, then in the S-Box table go to 4 in 'x' axis and 1 in 'y' axis to get S-box[0x41] -> 0x83 thus the contents of block[0] = 0x83

### shift_row:

The second stage of the round process executes a cyclical shift (rotate left) of the rows of the state table. The row number 0 is not affected, and the other rows are shifted according to Table 5:

### TABLE 5: ENCRYPTION CYCLICAL SHIFT TABLE

<table>
<thead>
<tr>
<th># shifts of row 1</th>
<th># shifts of row 2</th>
<th># shifts of row 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>16-byte block</td>
<td>1</td>
<td>2</td>
</tr>
<tr>
<td>24-byte block</td>
<td>1</td>
<td>2</td>
</tr>
<tr>
<td>32-byte block</td>
<td>1</td>
<td>3</td>
</tr>
</tbody>
</table>

### EXAMPLE 5: shift_row TRANSFORMATION

For the 16-byte block and key version (the implemented one), a state table with the following content:

<table>
<thead>
<tr>
<th>A</th>
<th>B</th>
<th>C</th>
<th>D</th>
</tr>
</thead>
<tbody>
<tr>
<td>E</td>
<td>F</td>
<td>G</td>
<td>H</td>
</tr>
<tr>
<td>I</td>
<td>J</td>
<td>K</td>
<td>L</td>
</tr>
<tr>
<td>M</td>
<td>N</td>
<td>O</td>
<td>P</td>
</tr>
</tbody>
</table>

Becomes the following after the shift_row transformation:

<table>
<thead>
<tr>
<th>A</th>
<th>B</th>
<th>C</th>
<th>D</th>
</tr>
</thead>
<tbody>
<tr>
<td>F</td>
<td>G</td>
<td>H</td>
<td>E</td>
</tr>
<tr>
<td>K</td>
<td>L</td>
<td>I</td>
<td>J</td>
</tr>
<tr>
<td>P</td>
<td>M</td>
<td>N</td>
<td>O</td>
</tr>
</tbody>
</table>
**mix_column:**
This operation, described in the AES Proposal (see Chapter 2 - Mathematical Preliminaries and Section 4.2.3 - The MixColumn Transformation), comprises the multiplication of each column of the state by a fixed matrix $c(x)$ following some special rules (Polynomials with coefficients in $\text{GF}(2^8)$), see Example 6.

The general form of this matrix multiplication is shown in the following equation:

<table>
<thead>
<tr>
<th>FIXED MATRIX $c(x)$</th>
<th>$a_0$</th>
<th>$a_1$</th>
<th>$a_2$</th>
<th>$a_3$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$b_0$</td>
<td>02</td>
<td>03</td>
<td>01</td>
<td>01</td>
</tr>
<tr>
<td>$b_1$</td>
<td>01</td>
<td>02</td>
<td>03</td>
<td>01</td>
</tr>
<tr>
<td>$b_2$</td>
<td>01</td>
<td>01</td>
<td>02</td>
<td>03</td>
</tr>
<tr>
<td>$b_3$</td>
<td>03</td>
<td>01</td>
<td>01</td>
<td>02</td>
</tr>
</tbody>
</table>

An example of matrix multiplication can be seen in Example 7.

**key_addition:**
This step takes the next round key and executes an XOR with the state in the form:

```c
for(i=0;i<16;i++)
    Block[i] ^= W[round+1][i];
```

---

### EXAMPLE 6: MATRIX MULTIPLICATION CONCEPTS USING SPECIAL RULES
First, let's define the $xtime$ operation:

if(a<0x80)
    a<<=1;
else
    a=(a<<1)^0x1B;

From this we can see that the $xtime$ operation for values lower than 0x80 is equivalent to a shift left (multiply by 2). For values bigger than or equal to 0x80, an extra XOR with 0x1B is necessary.

Multiply $c[i][0]=0xA7$ by $a[i]=0x0D$

Where

- $0xA7 \odot 0x01=0xA7$
- $0xA7 \odot 0x02=xtime(0xA7)=0x55; \ ((0xA7)<<1) ^0x1B)$
- $0xA7 \odot 0x04=xtime(xtime(0xA7))=0xAA; \ ((0x55)<<1)$
- $0xA7 \odot 0x08=xtime(xtime(xtime(0xA7)))=0x4F; \ ((0xAA)<<1) ^0x1B)$

Therefore, $0xA7 \odot 0x0D$ may be written as:

$(0xA7 \odot 0x01) \oplus (0xA7 \odot 0x04) \oplus (0xA7 \odot 0x08) = 0xA7 \oplus 0xAA \oplus 0x42$

The partial results are not added, but instead they are XORed to generate the new terms of the column.

**Note:** $\oplus$ means XOR.
EXAMPLE 7: MATRIX MULTIPLICATION

\[
\begin{array}{l}
\begin{array}{c|cccc}
  & b_0 & b_1 & b_2 & b_3 \\
\hline
 b_0 & 02 & 03 & 01 & 01 \\
 b_1 & 01 & 02 & 03 & 01 \\
 b_2 & 01 & 01 & 02 & 03 \\
 b_3 & 03 & 01 & 01 & 02 \\
\end{array}
\end{array}
\times
\begin{array}{c|c}
  & 5A & FD \\
\hline
 11 & 11 & 89 \\
\end{array}
\]

\[b_0 = 2 \cdot 5A \oplus 3 \cdot 11 \oplus 1 \cdot FD \oplus 1 \cdot 89\]
where
\[2 \cdot 5A = \text{xtime } (5A) = B4\]
\[3 \cdot 11 = 11 \oplus \text{xtime } (11) = 11 \oplus 22 = 0x33\]
\[1 \cdot FD = FD\]
\[1 \cdot 89 = 89\]
therefore
\[b_0 = B4 \oplus 33 \oplus FD \oplus 89 = F3\]

\[\hline\]
\[b_1 = 1 \cdot 5A \oplus 2 \cdot 11 \oplus 3 \cdot FD \oplus 1 \cdot 89\]
where
\[1 \cdot 5A = 5A\]
\[2 \cdot 11 = \text{xtime } (11) = 22\]
\[3 \cdot FD = FD \oplus \text{xtime } (FD) = FD \oplus E1 = 1C\]
\[1 \cdot 89 = 89\]
therefore
\[b_1 = 5A \oplus 22 \oplus 1C \oplus 89 = ED\]

\[\hline\]
\[b_2 = 1 \cdot 5A \oplus 1 \cdot 11 \oplus 2 \cdot FD \oplus 3 \cdot 89\]
where
\[1 \cdot 5A = 5A\]
\[1 \cdot 11 = 11\]
\[2 \cdot FD = \text{xtime } (FD) = E1\]
\[3 \cdot 89 = 89 \oplus \text{xtime } (89) = 80\]
therefore
\[b_2 = 5A \oplus 11 \oplus E1 \oplus 80 = 2A\]

\[\hline\]
\[b_3 = 3 \cdot 5A \oplus 1 \cdot 11 \oplus 1 \cdot FD \oplus 2 \cdot 89\]
where
\[3 \cdot 5A = 5A \oplus \text{xtime } (5A) = 5A \oplus B4 = EE\]
\[1 \cdot 11 = 11\]
\[1 \cdot FD = FD\]
\[2 \cdot 89 = \text{xtime } (89) = 09\]
therefore
\[b_3 = EE \oplus 11 \oplus FD \oplus 09 = 0B\]

Now, the general form of \(b[i] = c[i][0] \cdot a[0] \oplus c[i][1] \cdot a[1] \oplus c[i][2] \cdot a[2] \oplus c[i][3] \cdot a[3];\)

Observation1: The partial results are XORed (\(\oplus\)) instead of added.
Observation2: In this multiplication (\(\cdot\)), each time a carry bit occurs, the result must be XORed with 0x1B (xtime).
Key Schedule: Expansion and Selection: Decryption

In order to prepare for the round transformations, a “key schedule” operation must be executed. This function is basically the same as the one used in encryption; the difference is that, in the encryption process, the round keys are used in the direct order, W[0], W[1], W[2],..., while in the decryption process, they are used in the reverse order: W[10], W[9], W[8], ...

After the dec_key_schedule, an initial key addition must be executed:

Initial key_addition:

Before the first round of decryption, an initial key_addition is performed. This operation executes a simple XOR of the state with the final round key. In C (for 128-bit key and block):

```c
for(i=0;i<16;i++)
    Block[i] ^= W[10][i];
```

The Structure of the Round Transformations: Decryption

In the decryption process, each of the ten rounds (with the exception of the first one) is composed of four stages:

- byte_sub
- shift_row
- inv_mix_column
- key_addition

The first round doesn't execute the inv_mix_column stage, thus the sequence is:

- byte_sub
- shift_row
- key_addition
TABLE 6: SI-BOX OR DECRYPTION SUBSTITUTION TABLE (VALUES IN HEXADECIMAL)

<table>
<thead>
<tr>
<th>x</th>
<th>0</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
<th>A</th>
<th>B</th>
<th>C</th>
<th>D</th>
<th>E</th>
<th>F</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>52</td>
<td>09</td>
<td>6A</td>
<td>D5</td>
<td>30</td>
<td>36</td>
<td>A5</td>
<td>38</td>
<td>BF</td>
<td>40</td>
<td>A3</td>
<td>9E</td>
<td>91</td>
<td>F3</td>
<td>D7</td>
<td>FB</td>
</tr>
<tr>
<td>1</td>
<td>7C</td>
<td>E3</td>
<td>39</td>
<td>82</td>
<td>9B</td>
<td>2F</td>
<td>FF</td>
<td>87</td>
<td>34</td>
<td>8E</td>
<td>43</td>
<td>44</td>
<td>C4</td>
<td>DE</td>
<td>E9</td>
<td>CB</td>
</tr>
<tr>
<td>2</td>
<td>54</td>
<td>7B</td>
<td>94</td>
<td>32</td>
<td>A6</td>
<td>C2</td>
<td>23</td>
<td>3D</td>
<td>EE</td>
<td>4C</td>
<td>95</td>
<td>0B</td>
<td>42</td>
<td>FA</td>
<td>C3</td>
<td>4E</td>
</tr>
<tr>
<td>3</td>
<td>08</td>
<td>2E</td>
<td>A1</td>
<td>66</td>
<td>28</td>
<td>D9</td>
<td>24</td>
<td>B2</td>
<td>76</td>
<td>5B</td>
<td>A2</td>
<td>49</td>
<td>6D</td>
<td>8B</td>
<td>D1</td>
<td>25</td>
</tr>
<tr>
<td>4</td>
<td>72</td>
<td>F8</td>
<td>F6</td>
<td>64</td>
<td>86</td>
<td>68</td>
<td>98</td>
<td>16</td>
<td>D4</td>
<td>A4</td>
<td>5C</td>
<td>CC</td>
<td>5D</td>
<td>65</td>
<td>B6</td>
<td>92</td>
</tr>
<tr>
<td>5</td>
<td>6C</td>
<td>70</td>
<td>48</td>
<td>50</td>
<td>FD</td>
<td>ED</td>
<td>B9</td>
<td>DA</td>
<td>5E</td>
<td>15</td>
<td>46</td>
<td>57</td>
<td>A7</td>
<td>8D</td>
<td>9D</td>
<td>84</td>
</tr>
<tr>
<td>6</td>
<td>90</td>
<td>D8</td>
<td>AB</td>
<td>00</td>
<td>8C</td>
<td>BC</td>
<td>D3</td>
<td>0A</td>
<td>F7</td>
<td>E4</td>
<td>58</td>
<td>05</td>
<td>B8</td>
<td>B3</td>
<td>45</td>
<td>06</td>
</tr>
<tr>
<td>7</td>
<td>D0</td>
<td>2C</td>
<td>1E</td>
<td>8F</td>
<td>CA</td>
<td>3F</td>
<td>0F</td>
<td>02</td>
<td>C1</td>
<td>AF</td>
<td>BD</td>
<td>03</td>
<td>01</td>
<td>13</td>
<td>8A</td>
<td>6B</td>
</tr>
<tr>
<td>8</td>
<td>3A</td>
<td>91</td>
<td>11</td>
<td>41</td>
<td>4F</td>
<td>67</td>
<td>DC</td>
<td>EA</td>
<td>97</td>
<td>F2</td>
<td>CF</td>
<td>CE</td>
<td>F0</td>
<td>B4</td>
<td>E6</td>
<td>73</td>
</tr>
<tr>
<td>9</td>
<td>96</td>
<td>AC</td>
<td>74</td>
<td>22</td>
<td>E7</td>
<td>AD</td>
<td>35</td>
<td>85</td>
<td>E2</td>
<td>F9</td>
<td>37</td>
<td>E8</td>
<td>1C</td>
<td>75</td>
<td>DF</td>
<td>6E</td>
</tr>
<tr>
<td>A</td>
<td>47</td>
<td>F1</td>
<td>1A</td>
<td>71</td>
<td>1D</td>
<td>29</td>
<td>C5</td>
<td>89</td>
<td>6F</td>
<td>B7</td>
<td>62</td>
<td>0E</td>
<td>AA</td>
<td>18</td>
<td>BE</td>
<td>1B</td>
</tr>
<tr>
<td>B</td>
<td>FC</td>
<td>56</td>
<td>3E</td>
<td>48</td>
<td>C6</td>
<td>D2</td>
<td>79</td>
<td>20</td>
<td>9A</td>
<td>DB</td>
<td>C0</td>
<td>FE</td>
<td>78</td>
<td>CD</td>
<td>5A</td>
<td>F4</td>
</tr>
<tr>
<td>C</td>
<td>1F</td>
<td>DD</td>
<td>A8</td>
<td>33</td>
<td>88</td>
<td>07</td>
<td>C7</td>
<td>31</td>
<td>B1</td>
<td>12</td>
<td>10</td>
<td>59</td>
<td>27</td>
<td>80</td>
<td>EC</td>
<td>5F</td>
</tr>
<tr>
<td>D</td>
<td>60</td>
<td>51</td>
<td>7F</td>
<td>A9</td>
<td>19</td>
<td>B5</td>
<td>4A</td>
<td>0D</td>
<td>2D</td>
<td>E5</td>
<td>7A</td>
<td>9F</td>
<td>93</td>
<td>C9</td>
<td>9C</td>
<td>EF</td>
</tr>
<tr>
<td>E</td>
<td>A0</td>
<td>E0</td>
<td>3B</td>
<td>4D</td>
<td>AE</td>
<td>2A</td>
<td>F5</td>
<td>B0</td>
<td>C8</td>
<td>EB</td>
<td>BB</td>
<td>3C</td>
<td>83</td>
<td>53</td>
<td>99</td>
<td>61</td>
</tr>
<tr>
<td>F</td>
<td>17</td>
<td>2B</td>
<td>04</td>
<td>7E</td>
<td>BA</td>
<td>77</td>
<td>D6</td>
<td>26</td>
<td>E1</td>
<td>69</td>
<td>14</td>
<td>63</td>
<td>55</td>
<td>21</td>
<td>0C</td>
<td>7D</td>
</tr>
</tbody>
</table>

DESCRIPTION OF DECRYPTION STAGES:
byte sub:
In this stage, each byte of the block is replaced by the content of the Si-box at the position defined by the byte that is going to be substituted. In this case, the Si-box or substitution table, may be seen as a 256-byte invertible vector/matrix, used to map the substitution process in the inverse direction taken by the S-box.

This is equivalent to the following C language fragment:

```
for(i=0;i<BLOCKSIZE;i++)
    block[i]=Si_box[block[i]];
```

This relationship of boxes may be understood easily as follows:

```
S-box[i] = j
Si-box[j] = i
```

EXAMPLE 8: SI BOX SUBSTITUTION

If block[0] = 0x83, then in the Si-Box table, go to 8 in ‘x’ axis and 3 in ‘y’ axis to get Si-box[0x83] -> 0x41, thus the contents of block[0] = 0x41
shift_row:
The second stage of the round process executes a cyclical shift (rotate left) of the rows of the state. The row number 0 is not affected and the other rows are shifted according to Table 7:

**TABLE 7: DECRYPTION CYCLICAL SHIFT TABLE**

<table>
<thead>
<tr>
<th>Block Size</th>
<th># shifts of row 1</th>
<th># shifts of row 2</th>
<th># shifts of row 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>16 byte</td>
<td>3</td>
<td>2</td>
<td>1</td>
</tr>
<tr>
<td>24 byte</td>
<td>5</td>
<td>4</td>
<td>3</td>
</tr>
<tr>
<td>32 byte</td>
<td>7</td>
<td>5</td>
<td>4</td>
</tr>
</tbody>
</table>

**EXAMPLE 9: shift-row TRANSFORMATION**

For the 16-byte block and key version (the implemented one), a state with the following content:

<table>
<thead>
<tr>
<th>A</th>
<th>B</th>
<th>C</th>
<th>D</th>
</tr>
</thead>
<tbody>
<tr>
<td>F</td>
<td>G</td>
<td>H</td>
<td>E</td>
</tr>
<tr>
<td>K</td>
<td>L</td>
<td>I</td>
<td>J</td>
</tr>
<tr>
<td>P</td>
<td>M</td>
<td>N</td>
<td>O</td>
</tr>
</tbody>
</table>

Becomes the following after the shift_row transformation:

<table>
<thead>
<tr>
<th>A</th>
<th>B</th>
<th>C</th>
<th>D</th>
</tr>
</thead>
<tbody>
<tr>
<td>E</td>
<td>F</td>
<td>G</td>
<td>H</td>
</tr>
<tr>
<td>I</td>
<td>J</td>
<td>K</td>
<td>L</td>
</tr>
<tr>
<td>M</td>
<td>N</td>
<td>O</td>
<td>P</td>
</tr>
</tbody>
</table>

inv_mix_column:
The implementation follows the same rules applied to the mix_column routine, except the inv_mix_column uses the fixed matrix c(x) shown below. See the mix_column section under the description of Encryption Stages for an explanation of the matrix multiplication used in the AES algorithm.

\[
\begin{bmatrix}
0E & 0B & 0D & 09 \\
09 & 0E & 0B & 0D \\
0D & 09 & 0E & 0B \\
0B & 0D & 09 & 0E \\
\end{bmatrix}
\times
\begin{bmatrix}
a_0 \\
a_1 \\
a_2 \\
a_3 \\
\end{bmatrix}
\]

key_addition:

This step takes the next round key and executes an XOR with the state in the form: (NUMROUNDS=11 for 16-byte block).

\[
\text{for}(i=0;i<16;i++)
\text{Block}[i]^=\text{W[NUMROUNDS- rounds][i]};
\]
Program Structure

The general structure of the encryption program is:

```c
key_addition(block, key); // initial key addition
rounds = 10;
while ( rounds-- ) // loop 10x
{
    substitution_S(block);
    enc_shift_row(block);
    if( rounds != 1 ) // last round is done without mix_column
        mix_column(block);
    enc_key_schedule(key); // direct key_schedule executed on-the-fly
    key_addition(block, key);
}
```

The general structure of the decryption program is:

```c
init_decryption_key(key) // create the initial decryption key from initial key
rounds = 10;
key_addition(block, key); // initial
while ( rounds-- ) // loop 10x
{
    substitution_Si(block); // substitution with Si_box table
    dec_shift_row(block);
    if( rounds != 10 ) // first round is done without inv_mix_column
        inv_mix_column(block);
    dec_key_schedule(key); // inverse key_schedule executed on-the-fly
    key_addition(block, key);
}
```

mix_column Optimization

The original mix_column transformation, as described in the reference implementation of AES, is time consuming. Therefore, the following optimized equivalent form is recommended:

```c
for(i=0; i<4; i++)
{
    Tmp = block[i+0] ^ block[i+0x1] ^ block[i+0x2] ^ block[i+0x3];
    Block[i+0x0] ^= Tmp ^ xtime(block[i+0x0] ^ block[i+0x1])
    Block[i+0x1] ^= Tmp ^ xtime(block[i+0x1] ^ block[i+0x2])
    Block[i+0x2] ^= Tmp ^ xtime(block[i+0x2] ^ block[i+0x3])
    Block[i+0x3] ^= Tmp ^ xtime(block[i+0x3] ^ block[i+0x0])
}```
inv_mix_column Optimization

The original inv_mix_column transformation, as described in the reference implementation of AES, is time consuming, so the optimized equivalent form is used:

for(i=0;i<4;i++)
{
    Tmp0 = block[i+0] ^ block[i+0x1] ^ block[i+0x2] ^ block[i+0x3];
    Tmp1 = xtime(block[i+0] ^ block[i+0x2]);
    Tmp2 = xtime(block[i+1] ^ block[i+0x3]);
    Tmp3 = xtime( xtime( Tmp1 ^ Tmp2 ) ) ^ Tmp0;
    Block[i=0x0] ^= xtime(block[i+0x0]^block[i+0x1] ^ Tmp1) ^ Tmp3;
    Block[i+0x1] ^= xtime(block[i+0x1]^block[i+0x2] ^ Tmp2) ^ Tmp3;
    Block[i+0x2] ^= xtime(block[i+0x2]^block[i+0x3] ^ Tmp1) ^ Tmp3;
    Block[i+0x3] = block[i+0x0] ^ block[i+0x1] ^ block[i+0x2] ^ Tmp0
}

On-The-Fly Key Schedule

The original key schedule functions use several RAM positions, in order to save all round keys used in the encryption/decryption process.

To reduce the RAM consumption, the implementation of the round keys was done on-the-fly. To do this, three different functions were added:

1. enc_key_schedule(key): This function takes the actual key and generates the next round key that is placed in the same RAM positions.
2. dec_key_schedule(key): This function takes the actual key and generates the previous round key that is placed in the same RAM positions.
3. init_decryption_key(key): This function takes the initial key used to encrypt the code and executes the enc_key_schedule(key) function NUMROUNDS times. The result is the last round key used in the encryption.

The reason behind this is that in the encryption process, the rounds use the scheduled keys (W) in the following sequence:


While the decryption process uses the exact same scheduled keys in the reverse order:

Given the generic round key:

<table>
<thead>
<tr>
<th>K0</th>
<th>K4</th>
<th>K8</th>
<th>K12</th>
</tr>
</thead>
<tbody>
<tr>
<td>K1</td>
<td>K5</td>
<td>K9</td>
<td>K13</td>
</tr>
<tr>
<td>K2</td>
<td>K6</td>
<td>K10</td>
<td>K14</td>
</tr>
<tr>
<td>K3</td>
<td>K7</td>
<td>K11</td>
<td>K15</td>
</tr>
</tbody>
</table>

**enc_key Schedule:**

The enc_key schedule may be understood in four steps:

1. Column 0 is transformed as follows:

<table>
<thead>
<tr>
<th>K0 ^= s_box[K13]</th>
<th>K4</th>
<th>K8</th>
<th>K12</th>
</tr>
</thead>
<tbody>
<tr>
<td>K1 ^= s_box[K14]</td>
<td>K5</td>
<td>K9</td>
<td>K13</td>
</tr>
<tr>
<td>K2 ^= s_box[K15]</td>
<td>K6</td>
<td>K10</td>
<td>K14</td>
</tr>
<tr>
<td>K3 ^= s_box[K12]</td>
<td>K7</td>
<td>K11</td>
<td>K15</td>
</tr>
</tbody>
</table>

   After that:

   K0 = K0 ^ Rcon
   Rcon = xtime(Rcon)
   The startup value of Rcon =0x01

2. Column 1 is XORed with column 0 as follows:

   K4 ^= K0
   K5 ^= K1
   K6 ^= K2
   K7 ^= K3

3. Column 2 is XORed with column 1 as follows:

   K8 ^= K4
   K9 ^= K5
   K10 ^= K6
   K11 ^= K7

4. Column 3 is XORed with column 2 as follows:

   K12 ^= K8
   K13 ^= K9
   K14 ^= K10
   K15 ^= K11

**dec_key Schedule**

The dec_key schedule may be understood in the exact same steps executed in reverse order:

1. Column 3 is XORed with column 2 as follows:

   K12 ^= K8
   K13 ^= K9
   K14 ^= K10
   K15 ^= K11

2. Column 2 is XORed with column 1 as follows:

<table>
<thead>
<tr>
<th>K0 ^= s_box[K13]</th>
<th>K4</th>
<th>K8</th>
<th>K12</th>
</tr>
</thead>
<tbody>
<tr>
<td>K5 ^= s_box[K14]</td>
<td>K5</td>
<td>K9</td>
<td>K13</td>
</tr>
<tr>
<td>K6 ^= s_box[K15]</td>
<td>K6</td>
<td>K10</td>
<td>K14</td>
</tr>
<tr>
<td>K7 ^= s_box[K12]</td>
<td>K7</td>
<td>K11</td>
<td>K15</td>
</tr>
</tbody>
</table>

   And after that:

   K0 = K0 ^ Rcon
   if(Rcon & 0x01)
   Rcon = 0x80
   else
   Rcon >>= 1

   This procedure is the exact inverse operation executed over K0 in the enc_key process (i.e., the xtime function applied to Rcon).
Source Code Example 1 (Encryption and Decryption)

The `aes_rijn.asm` source code first encrypts 16 bytes of data, then decrypts the 16 bytes of data that were just encrypted. Listed below is some important information you should know before using this source code:

1. Source code is written in Microchip Assembly language (MPASM™ Assembler).
2. Source code in `aes_rijn.asm` has been tested using MPLAB® 5.20.00:
   - Simulator testing has been done using a PIC16C622A device.
   - MPLAB ICD testing has been done using a PIC16F870 device. When using this device, the `tables.inc` memory locations need to be adjusted to accommodate the MPLAB ICD memory needs.
3. The `tables.inc` file is listed in Appendix F. This is where the S-TABLE & Si-TABLE can be found.
4. ROM Memory needed for Example #1 is:
   - (1416 x 14 bits) instructions
5. RAM Memory needed for Example #1 is:
   - encryption: 38 bytes total
     - 16 for the block cipher
     - 16 for key
     - 6 for loop control and partial result calculation
   - decryption: 41 bytes total
     - 16 for the block cipher
     - 16 for key
     - 9 for loop control and partial result calculation

   **Note:** 41 bytes is the total needed; several registers are shared.

6. Execution Speed (in instruction cycles, calculated as the external clock/4):
   - encryption time: up to 5273 cycles
   - decryption schedule: up to 928 cycles
   - decryption time: up to 6413 cycles

   **Note:** The number of cycles shown here were the largest found during simulations. Depending on your code implementation, these times may vary.

7. The 16-byte block vector is located in RAM locations 0x20 - 0x2F:
   - The `set_test_block` subroutine of the `aes_rijn.asm` code loads the 16 bytes of hard coded plain text data into the block vector. In order to change the initial block vector data, the `set_test_block` code needs to be changed.
   - The block vector is where the plain text data resides before the encryption process. The block vector is also where the encrypted text resides after the encryption process and before the decryption process, and finally, where the plain text data resides after the decryption process. It is important to be aware that the block vector locations are overwritten during code execution.

8. The 16-byte key vector is located in RAM locations 0x30 - 0x3F:
   - The `set_test_key` subroutine of the `aes_rijn.asm` code loads the 16 bytes of hard coded key data into the key vector. In order to change the initial key vector data, the `set_test_key` code needs to be changed.

9. Test data can be found in the following files:
   - `ecbvt.txt` contains the encrypted results (CT) for changing plain text block vector data (PT) when the key vector data (KEY) is kept constant at KEY=0000000000000000
   - `ecbvk.txt` contains the encrypted results (CT) for changing key vector data (KEY) when the plain text block vector data (PT) is kept constant at PT=0000000000000000

10. The files you will need for this example are as follows:
    - `aes_rijn.asm`
    - `tables.inc`
    - `ecbvt.txt` (KEY constant)
    - `ecbvk.txt` (PT constant)

These files can be found with this Application Note on the Microchip web site:

   www.microchip.com

**Warning:** United States federal regulations allow the Advanced Encryption Standard (AES) software code to be downloaded from the Microchip web site. The United States federal regulations restrict transfer of this Advanced Encryption Standard (AES) software by other means such as e-mail.
Source Code Example 2 (Encryption)

The `aes_encr.asm` source code encrypts 16 bytes of data. Listed below is some important information you should know before using this source code:

1. Source Code is written in Microchip Assembly language (MPASM Assembler).
2. Source Code in `aes_encr.asm` has been tested using MPLAB 5.20.00:
   - Simulator testing has been done using a PIC16C622A device.
   - MPLAB ICD testing has been done using a PIC16F870 device. When using this device, the `tables.inc` memory locations need to be adjusted to accommodate the MPLAB ICD memory needs.
3. The `s_table.inc` file is where the S-TABLE can be found.
4. ROM Memory needed for Example #2 is:
   - encryption: (728 x 14 bit) instructions
5. RAM Memory needed for Example #2 is:
   - encryption: 38 bytes total
     16 for the block cipher
     16 for key
     6 for loop control and partial result calculation
6. Execution Speed (in instruction cycles, calculated as the external clock/4):
   - encryption time: up to 5273 cycles

**Note:** The number of cycles shown here were the largest found during simulations. Depending on your code implementation, these times may vary.

7. The 16-byte block vector is located in RAM locations 0x20 - 0x2F:
   - The `set_test_block` subroutine of the `aes_encr.asm` code loads the 16 bytes of hard coded plain text data into the block vector. In order to change the initial block vector data, the `set_test_block` code needs to be changed.
   - The block vector is where the plain text data resides before the encryption process. The block vector is also where the encrypted text resides after the encryption process. It is important to be aware that the block vector locations are overwritten during code execution.

8. The 16-byte key vector is located in RAM locations 0x30 - 0x3F:
   - The `set_test_key` subroutine of the `aes_encr.asm` code loads the 16 bytes of hard coded key data into the key vector. In order to change the initial key vector data, the `set_test_key` code needs to be changed.

9. Test data can be found in the following files:
   - `ecbvt.txt` contains the encrypted results (CT) for changing plain text block vector data (PT) when the key vector data (KEY) is kept constant at KEY=0000000000000000.
   - `ecbvk.txt` contains the encrypted results (CT) for changing key vector data (KEY) when the plain text block vector data (PT) is kept constant at PT=0000000000000000.

10. The files you will need to run and test this Example are as follows:
    - `aes_encr.asm`
    - `s_table.inc`
    - `ecbvt.txt` (KEY constant)
    - `ecbvk.txt` (PT constant)

These files can be found with this Application Note on the Microchip web site: [www.microchip.com](http://www.microchip.com)

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Source Code Example 3 (Decryption)

The aes_decr.asm source code decrypts the 16 bytes of data. Listed below is some important information you should know before using this source code:

1. Source Code is written in Microchip Assembly language (MPASM Assembler).
2. Source Code aes_decr.asm has been tested using MPLAB 5.20.00:
   - Simulator testing has been done using a PIC16C622A device. When using this device, the tables.inc memory locations need to be adjusted to accommodate the MPLAB ICD memory needs.
   - ICD testing has been done using a PIC16F870 device.
3. The tables.inc file is listed in Appendix F. This is where the S-TABLE and Si-TABLE can be found.
4. ROM Memory needed for Example #3 is:
   - 1143 x 14 bit instructions
5. RAM Memory needed for Example #3 is:
   - decryption: 41 bytes total
     16 for the block cipher
     16 for key
     9 for loop control and partial result calculation
   - decryption schedule: up to 928 cycles
   - decryption time: up to 6413 cycles

Note: The number of cycles shown here were the largest found during simulations. Depending on your code implementation, these times may vary.

6. The 16-byte block vector is located in RAM locations 0x20 - 0x2F:
   - The set_test_block subroutine of the aes_decr.asm code loads the 16 bytes of hard coded plain text data into the block vector.
   - In order to change the initial block vector data, the set_test_block code needs to be changed.
   - The block vector is where the encrypted text data resides before the decryption process. The block vector is also where the plain text data resides after the decryption process. It is important to be aware that the block vector locations are overwritten during code execution.
7. The 16-byte key vector is located in RAM locations 0x30 - 0x3F:
   - The set_test_key subroutine of the aes_decr.asm code loads the 16 bytes of hard coded key data into the key vector.
8. The 16-byte key vector is located in RAM locations 0x30 - 0x3F:
   - The set_test_key subroutine of the aes_decr.asm code loads the 16 bytes of hard coded key data into the key vector.
9. Appendix H and Appendix I hold test data:
   - ecbvt.txt contains the encrypted results (CT) for changing plain text block vector data (PT) when the key vector data (KEY) is kept constant at KEY=0000000000000000.
   - ecb_vk.txt contains the encrypted results (CT) for changing key vector data (KEY) when the plain text block vector data (PT) is kept constant at PT=0000000000000000.
10. The files you will need to run and test this example are as follows:
    - aes_decr.asm
    - tables.inc
    - ecbvt.txt (KEY constant)
    - ecbvk.txt (PT constant)

These files can be found with this Application Note on the Microchip web site:

www.microchip.com

Warning: United States federal regulations allow the Advanced Encryption Standard (AES) software code to be downloaded from the Microchip web site. The United States federal regulations restrict transfer of this Advanced Encryption Standard (AES) software by other means such as e-mail.
References

- Internet: Several good sources of information about Cryptography, in general, and AES/Rijndael were used in this Application Note:
  - NIST: http://csrc.nist.gov/encryption/aes/aes_home.htm
  - Rijndael home page:http://www.esat.kuleuven.ac.be/~rijmen/rijndael
  - Ritter: http://www.io.com/~ritter
  - Savard: http://home.ecn.ab.ca/~jsavard/crypto


- Implementations: Excellent implementations were consulted and studied during the development process and to them our acknowledgement and gratitude:
  - Paulo Barreto, Dr. Vincent Rijmen and Antoon Bosselaers for their references and fast C versions of Rijndael.
  - Dr. Brian R. Gladman for his C++ implementation.
  - Mike Scott by his C version.
  - Rafael R. Sevilla for his 80x86 assembly version.
  - Robert G. Durnal for his 80x86 assembly version.
APPENDIX A: AES ENCRYPTION FLOW CHART

1. Get block to be Ciphered and ciphering key
2. Initiate ROUND_COUNTER value = 10
3. Key addition
4. Substitution S
5. Enc_shift_row
6. Check if ROUND_COUNTER = 1
   - True: Mix column
   - False: Enc_key_schedule → Key addition
7. Decrement ROUND_COUNTER
8. Check if ROUND_COUNTER = 0
   - True: END
   - False: Go back to step 4
APPENDIX B: AES DECRYPTION FLOW CHART

1. **DECRIPTION**
2. Get block to be deciphered and ciphering key
3. Initiate `ROUND_COUNTER` value = 10
4. key_addition
5. substitution_Si
6. dec_shift_row

- If `ROUND_COUNTER = 10`?
  - True
  - inv_mix_column
  - dec_key_schedule
  - key_addition
  - Decrement `ROUND_COUNTER`

- If `ROUND_COUNTER = 0`?
  - True
  - END

- False
  - False
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